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Database Design Appendix C, app3.tex
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## Appendix C

## Symbols Used

## Mathematical Symbols Used

| $\rceil$ | CEIL, next higher integer |
| :---: | :---: |
| \」 | FLOOR, next lower integer |
| $\approx$ | approximately equal |
| $\ddot{\text { ü }}$ | much greater than |
| ! | factorial |
| \# | number of |
| $\log _{y} x$ | logarithm base $y$ of $x$ |
| $\log x$ | natural logarithm of $x$, base $e=2.71828182846$ |
| $\sum_{k} f(k)$ | sum of all $f(k)$ for the integer $k$ 's specified |
| $\ominus$ | one of the comparison operators $>\geq=\neq \leq<$ |
| $\wedge$ | and, true if both sides are true |
| V | or, true if either side is true |
|  | where, precedes a conditional clause |
| $\bigcap$ | set intersection |
| $\bigcup$ | set union |
| - | set difference |
| $\times$ | cartesian product |
| 5 | select tuples from a relation |
| $\Pi$ | project attributes from a relation |
| $\underset{a=b}{\infty}$ | join two relations based on equality of the attributes $a, b$ |
| $\succ$ | reference connection |
| * | ownership connection |
| $\longrightarrow$ | subset connection |
| $\subset$ | subset of |
| $\epsilon$ | member of |
| $\forall$ | for all |
| $\Rightarrow$ | becomes |
| \{ \} | enclose a set |
| [ ] | enclose a reference |

## Programming and Syntax Symbols As Used

In general we follow the convention of PL/1, a language originally developed by IBM to serve both scientific and commercial programming tasks. Some examples use Ada. a language sponsored by the US Defense department, COBOL, a widely used commercial language, and Pascal, a popular language for teaching.

| $a+b$ | addition |
| :---: | :---: |
| $\mathrm{a}-\mathrm{b}$ | subtraction |
| $\mathrm{a} * \mathrm{~b}$ | multiplication |
| $\mathrm{a} / \mathrm{b}$ | division |
| $\operatorname{MOD}(\mathrm{a}, \mathrm{b})$ | modulo, integer remainder of division |
| $\mathrm{a} * * \mathrm{~b}$ | exponentiation, a to the power b |
| $\mathrm{a}=\mathrm{b}$ | depending on context in PL/1, assignment or equality comparison |
| $\mathrm{a}>\mathrm{b}$ | greater than comparison, true if a greater than b |
| $\mathrm{a} \geq \mathrm{b}$ | greater or equal comparison, true if a greater or equal to b |
| $\mathrm{a} \wedge \mathrm{b}$ | and, true if both a, b true ( \& in PL/1) |
| $\mathrm{a} \vee \mathrm{b}$ | or, true if either a, b true ( 1 in PL/1) |
| $\neg \mathrm{c}$ | not, true if c false and vice versa ( $\neq$ in Ada, Pl/1) |
| s \\| w | catenation, string w appended to string s (\& in Ada) |
| s \| c | where, do s if the predicate (conditional) clause c is true |
| $R \bigcup S$ | union of relations R and S |
| $R \bigcap S$ | intersection of relations $R$ and $S$ |
| $R \times S$ | cross product of relations R and S |
| $\mathrm{R}-\mathrm{S}$ | difference, remove tuples matching $S$ from $R$ |
| SR.ex | select tuples of R according to expression ex |
| $\Pi$ R.a | projection of attributes a of R |
| R.aゆ\S.b | Join $R$ and $S$, on equality of attribute values in $a$ and $b$ |
| R.al $\triangle$ lS ${ }^{\text {b }}$ | Outerjoin including all tuples |
|  | field separator |
| :> | key and goal fields separator |
| ; | statement separator |
|  | termination of computational section |
| ss, | section ss may be repeated |
| [ ss ] | section ss is optional |
| \{ss/tt\} | sections ss, tt are alternatives |
| ::= | is defined by |
| /* Note */ | explanatory comments |
| a.b | qualification of variable b by a higher-level variable a,i.e., employee.name |
| "Word" | character string constant |
| - | (underline) pseudo-alphabetic character without syntactic meaning used for legibility within variable names. (In совоl - is used for this function.) |

## Variables Used in Performance Formulas

| A | average space required for attribute name | Sec. 3-1-3 |
| :---: | :---: | :---: |
| $a$ | number of different attributes in a file | Sec. 3-1-1 |
| $a^{\prime}$ | average number of attributes in a record | Sec. 3-1-1, 3-6-3 |
| $B$ | blocksize | Sec. 2-2 |
| $b$ | blockcount | Sec. 2-2-2 |
| $b t t$ | block transfer time $=B / t$ | Eq. 2-13 |
| $B f r$ | blocking factor $\approx B / R$ | Eqs. 2-5, 2-6, 2-7, 2-20 |
| C | Cost factors | Sec. 5-4-6, 5-5-2 |
| c | computational overhead per record, when not negligible | le Sec. 2-3-4 |
| D | space required for data | Eq. 5-1, Sec 5-3-3 |
| d | number of records that have been invalidated | Sec. 3-1-3 |
| $F$ | subscript denoting a fetch for a specific record | Sec. 3-0-2 |
| $G$ | space required for an interblock gap | Sec. 2-2-3 |
| $h$ | classification variable | Sec. 5-4-3 |
| I | subscript denoting insertion of a record | Sec. 3-0-2 |
| j | number of cylinders | Sec. 2-2-1 |
| K | projection list | Sec. 7-3-2 |
| K | Kilo or thousand (1024) times |  |
| $k$ | number of tracks per cylinder | Sec. 2-2-5, Table 2-1 |
| $L$ | load frequency factors; selection list | Sec. 5-1; 7-3-3 |
| M | multiprogramming factor | Eq. 5-19 |
| M | Mega or million (1048576) times |  |
| $m$ | number of available slots for records | Sec. 3-5-1 |
| $N$ | subscript denoting getting the next serial record | Sec. 3-0-2 |
| $n$ | number of records in a file | Sec. 3-1-3 |
| $o$ | number of records that overflow Secs. 3-1 | 3-1-3, 3-2-3, 3-3-3, 3-5-3 |
| $P$ | space required for a pointer | Sec. 2-3-3 |
| $p$ | collision cost, also probability Eqs. 3-73 | 3-73, 3-74, 3-79, Fig. 3-23 |
| $q$ | production demand by a file application | Eq. 5-2, 5-4 to 5-6 |
| $R$ | space required for a complete record; relation | Sec. 3-0-2; 7-1-1 |
| RW | subscript indicating rewriting | Sec. 2-3-6 |
| $r$ | rotational latency time | Eq. 2-3 |
| SI | storage space for index | Eq. 3-52 |
| $s$ | average seek time | Eq. 2-2 |
| $s^{\prime}$ | effective seek time | Eqs. 2-15, 2-16 |
| T | the time required for various operations; set of tuples | Sec. 3-0-2; 7-3 |
| $T_{\text {sort }}$ | the time required to sort a file | Eq. 3-11 |
| $t$ | transfer rate from a storage unit to processing memory | y Sec. 2-2-5 |
| $t^{\prime}$ | bulk transfer rate | Eqs. 2-17, 2-18, 2-19 |
| U | subscript denoting an update of a record | Sec. 3-0-2 |
| $u$ | utilization Eqs. | Eqs. 5-3, 5-7 to 5-18, 5-20 |
| $u f$ | utilization factor | Eqs. 6-25, 6-29 |
| $V$ | average space for value part of an attribute | Sec. 3-1-3 |
| $v$ | number of records updated | Sec. 3-2-3 |
| $w$ | wait time in queues | Eq. 6-26 |
| W | wasted space due to gaps per record Eq | Eqs. 2-9, 2-10, 2-11, 2-21 |
| $X$ | subscript denoting an exhaustive search | Sec. 3-0-2 |
| $x$ | number of levels in an index structure, master level | Eq. 3-27, 3-49, 3-97 |
| Y | subscript denoting a reorganization of a file | Sec. 3-0-2 |
| $y$ | fanout ratio | Eq. 3-26, 3-48 |

