CS347

Lecture 8 May 7, 2001 ©Prabhakar Raghavan

Today's topic

• Clustering documents

Why cluster documents

- Given a corpus, partition it into groups of related docs
 - Recursively, can induce a tree of topics
- Given the set of docs from the results of a search (say *jaguar*), partition into groups of related docs
 - semantic disambiguation

Results list clustering example



What makes docs "related"?

- Ideal: semantic similarity.
- Practical: statistical similarity
 - We will use cosine similarity.
 - Docs as vectors.
 - For many algorithms, easier to think in terms of a *distance* (rather than <u>similarity</u>) between docs.
 - We will describe algorithms in terms of cosine distance

Recall doc as vector

- Each doc *j* is a vector of *tf×idf* values, one component for each term.
- Can normalize to unit length.
- So we have a vector space
- terms are axes
- -n docs live in this space
- even with stemming, may have 10000+ dimensions





Two flavors of clustering

- Given *n* docs and a positive integer *k*, partition docs into *k* (disjoint) subsets.
- Given docs, partition into an "appropriate" number of subsets.
 - E.g., for query results ideal value of k not known up front.
- Can usually take an algorithm for one flavor and convert to the other.



Outliers in centroid computation • Ignore outliers when computing centroid. - What is an outlier? • Distance to centroid > M × average. Say 10. • Outlier

Agglomerative clustering

- Given target number of clusters *k*.
- Initially, each doc viewed as a cluster start with *n* clusters;
- Repeat:
 - while there are > k clusters, find the "closest pair" of clusters and merge them.

"Closest pair" of clusters

- Many variants to defining closest pair of clusters.
- Closest pair ⇔ two clusters whose centroids are the most cosine-similar.





Exercise

• Consider agglomerative clustering on *n* points on a line. Explain how you could avoid *n*³ distance computations - how many will your scheme use?



Different algorithm: k-means

- Iterative algorithm.
- More locality within each iteration.
- Hard to get good bounds on the number of iterations.

Basic iteration

- At the start of the iteration, we have *k* centroids.
 - Need not be docs, just some *k* points.
- Each doc assigned to the nearest centroid.
- All docs assigned to the same centroid are averaged to compute a new centroid;
 - thus have k new centroids.







Termination conditions Several possibilities, e.g., A fixed number of iterations. Centroid positions don't change. Does this mean that the docs in a cluster are unchanged? Why should the *k*-means algorithm ever reach a *fixed point*? A state in which clusters don't change. *k*-means is a special case of a general procedure known as the *EM algorithm*. Under reasonable conditions, known to converge. Number of iterations could be large.

Exercise

- Consider running 2-means clustering on a corpus, each doc of which is from one of two different languages. What are the two clusters we would expect to see?
- Is agglomerative clustering likely to produce different results?

Multi-lingual docs

- Canadian/Belgian government docs.
- Every doc in English and equivalent French.
 - Cluster by concepts rather than language.
 - Cross-lingual retrieval.

k not specified in advance

- Say, the results of a query.
- Solve an optimization problem: penalize having lots of clusters
 - compressed summary of list of docs.
- Tradeoff between having more clusters (better focus within each cluster) and having too many clusters

k not specified in advance

- Given a clustering, define the <u>Benefit</u> for a doc to be the cosine similarity to its centroid
- Define the <u>Total Benefit</u> to be the sum of the individual doc Benefits.

Why is there always a clustering of Total Benefit n?

Penalize lots of clusters

- For each cluster, we have a <u>Cost</u> C.
- Thus for a clustering with *k* clusters, the <u>Total Cost</u> is *kC*.
- Define the <u>Value</u> of a cluster to be =
 Total Benefit Total Cost.
- Find the clustering of highest Value, over all choices of *k*.

Back to agglomerative clustering

- In a run of agglomerative clustering, we can try all values of *k*=*n*,*n*-*1*,*n*-*2*, ... *1*.
- At each, we can measure our Value, then pick the best choice of *k*.

Exercises

• Suppose a run of agglomerative clustering finds *k*=7 to have the highest Value amongst all *k*. Have we found the highest-Value clustering amongst all clusterings with *k*=7?

Using clustering in applications

Clustering to speed up scoring

- From Lecture 4, recall sampling and pregrouping
 - Wanted to find, given a query *Q*, the nearest docs in the corpus
 - Wanted to avoid computing cosine similarity of Q to each of n docs in the corpus.

Sampling and pre-grouping (Lecture 4)

- First run a pre-processing phase:
 - pick \sqrt{n} *docs* at random: call these *leaders*
 - For each other doc, pre-compute nearest leader
 - Docs attached to a leader: its *followers;*Likely: each leader has ~ √n followers.
 - $\sim \underline{\text{Likery}}$. each leader has $\sim \sqrt{n}$ follows
- Process a query as follows:
 - Given query Q, find its nearest *leader L*.
 - Seek nearest docs from among *L*'s followers.

Instead of random leaders, cluster

- First run a pre-processing phase:
 - Cluster docs into \sqrt{n} clusters.
 - For each cluster, its centroid is the *leader*.
- Process a query as follows:
 - Given query Q, find its nearest leader L.
 - Seek nearest docs from among *L*'s followers.

Navigation structure

- Given a corpus, agglomerate into a hierarchy
- Throw away lower layers so you don't have *n* leaf topics each having a single doc.



Navigation structure

- Deciding how much to throw away needs human judgement.
- Can also induce hierarchy top-down e.g., use *k*-means, then recur on the clusters.
- Topics induced by clustering need human ratification.
- Need to address issues like partitioning at the top level by language.

Major issue - labelling

- After clustering algorithm finds clusters how can they be useful to the end user?
- Need pithy label for each cluster
 - In search results, say "Football" or "Car" in the *jaguar* example.
 - In topic trees, need navigational cues.Often done by hand, a posteriori.

Labeling

- Common heuristics list 5-10 most frequent terms in the centroid vector.
 - Drop stop-words; stem.
- Differential labeling by frequent terms
 - Within the cluster "Computers", child clusters all have the word *computer* as frequent terms.
 - Discriminant analysis of centroids for peer clusters.

Supervised vs. unsupervised learning

- Unsupervised learning:
 - Given corpus, infer structure implicit in the docs, without prior training.
- Supervised learning:
 - Train system to recognize docs of a certain type (e.g., docs in Italian, or docs about religion)
 - Decide whether or not new docs belong to the class(es) trained on

Resources

• Good demo of results-list clustering: <u>cluster.cs.yale.edu</u>