

# CS347

Lecture 11  
May 16, 2001  
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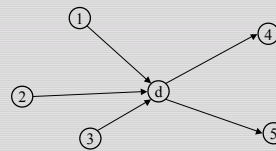
## Topics

- Link-based clustering
- Enumerative clustering/trawling
- Recommendation systems

## Link-based clustering

- Given docs in hypertext, cluster into  $k$  groups.
- Back to vector spaces!
- Set up as a vector space, with axes for terms as well as for in- and out-neighbors.

## Example



	1 2 3 4 5 ...	1 2 3 4 5 ...
Vector of terms in $d$	1 1 1 0 0 ...	0 0 0 1 1 ...
	In-links	Out-links

## Clustering

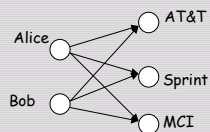
- Given vector space representation, run any of the clustering algorithms from lecture 8.
- Has been implemented on web search results.
- Other corpora: patents, citation structures.

## Back up

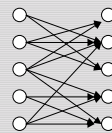
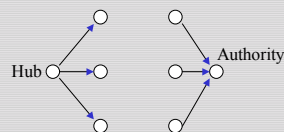
- In clustering, we partition input docs into clusters.
- In *trawling*, we'll enumerate subsets of the corpus that "look related"
  - will discard lots of docs
- Twist: will use purely link-based cues to decide whether docs are related

## Trawling/enumerative clustering

- In hyperlinked corpora - here, the web
- Look for all occurrences of a linkage pattern
- Recall from hubs/authorities search algorithm:



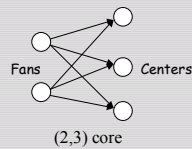
## Insights from hubs



Link-based hypothesis:  
Dense bipartite  
subgraph  $\Rightarrow$  web  
community.

## Communities from cores

- not easy, since web is huge
- what is a “dense subgraph”?
- define  $(i,j)$ -core: complete bipartite subgraph with  $i$  nodes all of which point to each of  $j$  others



## Random graphs inspiration

Every “large” enough “dense” bipartite graph “almost surely” has “non-trivial” core

e.g.,:

large = 3 by 10

dense = 50% edges

almost surely = 90% chance

non-trivial = 3 by 3

## Approach

- Find all  $(i,j)$ -cores ( $3 \leq i \leq 10$ ,  $3 \leq j \leq 20$ ).
- Expand each core into its full community.

## Finding cores

- “SQL” solution: find all triples of pages such that intersection of their outlinks is at least 3? Too expensive.
- Iterative pruning techniques actually work!

## Initial data & preprocessing

- Crawl, then extract links
- Work with potential fans:  
nodes with  $\geq j$  non-reciprocal links
- Eliminate mirrors
- Represent URLs by  $2 \times 32 = 64$ -bit hash
- Can sort URL's by either source or destination using disk-run sorting



## Popular page elimination

- Don't want "popular" communities (Yahoo!, Excite, DejaNews, webrings, ...)
- Popular community has popular page(s)
- Define popular page: indegree  $\geq 50$

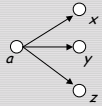
## Main requirements

- Main memory conservation
- Few disk passes over data

## Simple iterative pruning

- Discard all pages of in-degree  $< i$  or out-degree  $< j$ .
- Repeat 
- Reduces to a sequence of sorting operations  on the edge list

## Elimination/generation pruning



$a$  is part of a  $(3, 3)$  core if and only if the intersection of inlinks of  $x$ ,  $y$ , and  $z$  is at least 3

- pick a node  $a$  of degree 3
- for each  $a$  output neighbors  $x, y, z$
- use an index on centers to output in-links of  $x, y, z$
- intersect to decide if  $a$  is a fan
- at each step, either eliminate a page ( $a$ ) or generate a core

## Exercise

- Work through the details of maintaining the index on centers to speed up elimination-generation pruning.

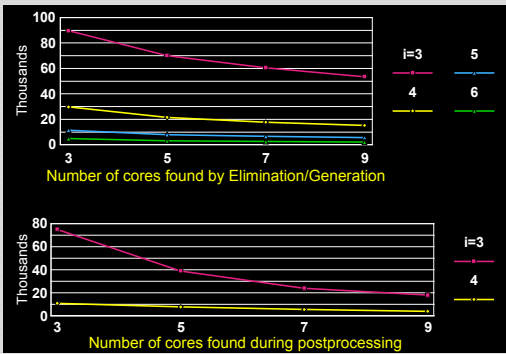
## Results after pruning

- Elimination/generation pruning yields >100K non-overlapping cores for small  $i, j$ .
- 5M unpruned edges
  - small enough for post-processing by *a priori*
  - build  $(i+1, j)$  cores from  $(i, j)$  cores

## Exercise

- Adapt the *a priori* algorithm to enumerating bipartite cores.

## Results for cores



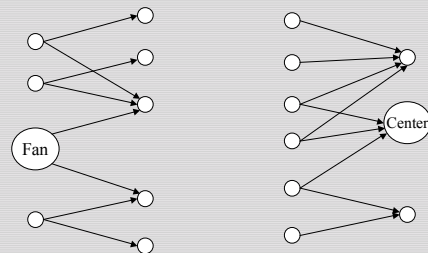
## Sample cores

- hotels in Costa Rica
- clipart
- Turkish student associations
- oil spills off the coast of Japan
- Australian fire brigades
- aviation/aircraft vendors
- guitar manufacturers

## From cores to communities

- Use hubs/authorities algorithm without text query - use fans/centers as samples
- Augment core with
  - all pages pointed to by any fan
    - all pages pointing into these
  - all pages pointing into any center
    - all pages pointed to by any of these

## Using sample hubs/authorities



## Costa Rican hotels and travel

- The Costa Rica International on arts, busi...
- Informatica Internacional de Costa Rica
- Cocos Island Research Center
- Aero Costa Rica
- Hotel Tilawa - Home Page
- COSTA RICA BY INTER@MERICA
- tamarindo.com
- Costa Rica
- New Page 5
- The Costa Rica Internet Directory.
- Costa Rica, Zarpe Travel and Casa Maria
- Si Como No Resort Hotels & Villas
- Apartotel El Sesteo... de San José, Cos...
- Spanish Abroad, Inc. Home Page
- Costa Rica's Pura Vida...ry - Reservation ...
- YELLOW\RESPALDO\HOTELS\Orquide1
- Costa Rica - Summary Profile
- COST RICA, MANUEL A...EPOS: VILLA
- Hotels and Travel in Costa Rica
- Nosara Hotels & Res...els & Restaurants...
- Costa Rica Travel, Tourism & Resorts
- Association Civica de Nosara
- Untitled:  
http://www...ca/hotels/mimos.html
- Costa Rica, Healthy...t Pura Vida
- Domestic & International Airline
- HOTELES / HOTELS - COSTA RICA
- touregems
- Hotel Tilawa - Links
- Costa Rica Hotels T...On line
- Reservations
- Yellow pages Costa ...Rica Export
- INFOHUB Costa Rica Travel Guide
- Hotel Parador, Manuel Antonio, Costa Rica
- Destinations

## Muslim student orgs.

- USC Muslim Students...ation Islamic Server
- The University of O...a Domain Name Change
- Caltech Muslim Students Home Page
- Islamic Society of Stanford University
- University of Texas...nformation Center...
- CSUN Muslim Students Association homepage
- HUDA
- Islamic Gateway
- Muslim Students' As...iversity of Michigan
- About Islam and Muslims
- Carnegie Mellon Uni...m Students Home Page
- Bookstore: The Onli...slamic Books, Isl...
- Islamic Texts and R... University at Bu...
- University of Warwick Islamic Society
- Muslim Students Ass...at Lehigh University
- MSA of CSU
- El Sagrado Corán
- Islamic Association... Palestine Home Page
- Kutkut - Islam
- Other MSAs and Organizations
- Other Resources rel...iversity at Buffal...
- 777
- Huma's Mamalist of Islamic Links!
- Other MSAs
- ZUBAIR'S ISLAM PAGE
- MIDDLE EAST CONFLICTS
- Islamic Links at the Arabic Paper
- Middle East & Arab Hot Links
- MSA National: MSAs Home Page
- Islamic Page
- Info about Muslims (MSA @SUNY/Bufalo)
- Untitled:  
http://www...ev/mideast/islam.htm
- Aalim Fevens: Islam Home Page
- islam
- Links to MSAs
- THE ISLAM PAGE

## Recommendation systems

## Recommendation Systems

Recommend docs to user based on user's context (besides the docs' content).

Other applications:

- Re-rank search results.
- Locate experts.
- Targeted ads.

## Input

Past transactions from users:

- which docs viewed
- which products purchased
- pages bookmarked....
- explicit ratings (movies, books....)

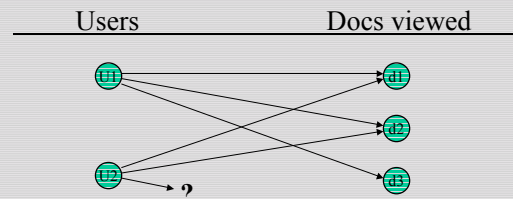
Current context:

- browsing history
- search(es) issued

Explicit profile info:

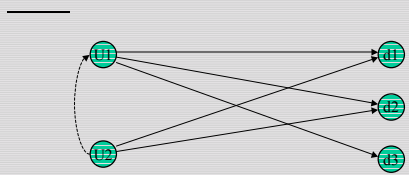
- Role in an enterprise
- Demographic info
- Interest profiles

## Example



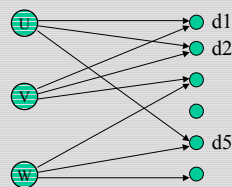
U1 viewed d1, d2, d3.  
U2 views d1, d2.  
Recommend d3 to U2.

## Expert finding



In an enterprise setting, recommend U1 to U2 as an expert.

## Simple Algorithm



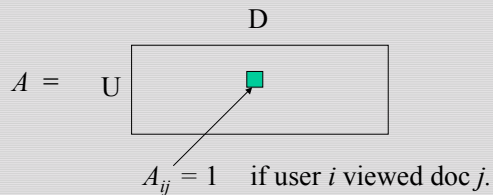
U viewed d1, d2, d5.

Look at who else viewed d1, d2 or d5.

Recommend to U the doc(s) most "popular" among these users.



### More formally



$AA^t$  : Entries give # of docs viewed by pairs of users.

### Voting Algorithm

- Row  $i$  of  $AA^t$  : Vector whose  $j^{\text{th}}$  entry is the # of docs viewed by both  $i$  and  $j$ .
- Call this row  $r_i$ , e.g., (0, 7, 1, 13, 0, 2, ...)
- Then  $r_i \circ A$  is a vector whose  $k^{\text{th}}$  entry gives a vote count to doc  $k$ 
  - emphasizes users who have high weights in  $r_i$ .
- Output doc(s) with highest vote counts.

What's on the diagonal of  $AA^t$ ?

### Voting Algorithm - implementation issues

- Wouldn't implement using matrix operations
  - use weight-propagation on data structures.
- Need to log and maintain “user views doc” relationship.
  - typically, log into database
  - update vote-propagating structures periodically.
- For efficiency, discard all but the heaviest weights in each  $r_i$ .

### What good was the matrix formulation?

- $AA^t$  entries give us a similarity measure between users.
- $r_i$  has proximities from user  $i$  to the rest.
- $r_i \circ A$  gives proximities from user  $i$  to the docs.

## Need a more general formulation

- If a user is close to two docs d1 and d2, are the docs d1 and d2 close to each other?
- How do we combine different sources of content and context?
  - terms in docs
  - links between docs
  - users' access patterns
  - users' info.

## Vector spaces again

Turn every entity into a vector.

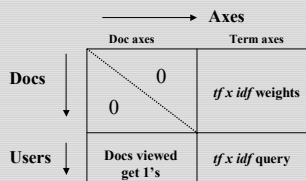
Axes are terms, docs, user info ...

e.g.,

- Some axes for terms
- One axis for each doc.
- Additional axes for user attributes like gender, enterprise role, etc.

## Vector Space

Each doc represented by  $tf \times idf$  weights for terms, plus a 1 entry for its own axis, and 0's elsewhere.



Users represented by 1's for docs viewed, 0's elsewhere.  
User posing a query:  $tf \times idf$  weights for terms.

## Context with content

- Docs' content captured in term axes.
- Other attributes (user behavior, current query etc.) captured in other axes.
- A probe consists of
  - 1 : a vector  $v$  (say, a user vector plus a query)
  - 2 : a type of vector to be retrieved (say, a doc)
- Result = vectors of chosen type closest to  $v$

## Implementation details

- Don't really want to maintain this gigantic (and sparse) vector space
- Dimension reduction
- Fast near neighbors (of vectors from a given type)
- Incremental versions needed

## Resources

- Hypertext clustering: D.S. Modha, W.S. Spangler. Clustering hypertext with applications to web searching.  
<http://citeseer.nj.nec.com/272770.html>
- Duplicate detection: A. Broder, S. Glassman, M. Manasse, and G. Zweig. Syntactic clustering of the Web.  
<http://citeseer.nj.nec.com/context/109312/0>
- *a priori* algorithm: R. Agrawal, R. Srikant. Fast algorithms for mining association rules.  
<http://citeseer.nj.nec.com/agrawal94fast.html>
- Trawling: S. Ravi Kumar, P. Raghavan, S. Rajagopalan and A. Tomkins. Trawling emerging cyber-communities automatically.  
<http://citeseer.nj.nec.com/context/843212/0>